# Boosting the MOSFETs Matching by Using Diamond Layout Style 

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#### Abstract

This manuscript presents an experimental comparative study between the Metal-Oxide-Semiconductor (MOS) Silicon-On-Insulator (SOI) Field Effect Transistors, n-type, (nMOSFETs) matching, which are implemented with the hexagonal gate shape (Diamond) and standard rectangular ones. The main analog parameters and figures of merit of 360 devices are investigated. The results establish that the Diamond SOI MOSFETs with $\alpha$ angles equal to 900 can boost in more than in average $\mathbf{- 4 5 . 8 \%}$ with a standard deviation of $\mathbf{2 0 . 1 \%}$ the devices matching in comparison to those found with the typical rectangular SOI MOSFETs, concerning the same gate area and bias conditions. Consequently, the Diamond layout style is an alternative technique to reduce the nMOSFETs' mismatching, considering the analog SOI Complementary MOS (CMOS) integrated circuits (ICs) applications.


Index Terms- Devices Matching, SOI nMOSFET and analog SOI CMOS ICs.

## I. Introduction

The electrical performance of analog Complementary Metal-Oxide-Semiconductor (CMOS) integrated circuits (ICs) is absolutely affected by the layouts of semiconductor devices (dimensions, geometric shape and how they are realized along the silicon wafer) [1-9]. Analog electrical performance of CMOS ICs may be also degraded when the devices dimensions are reduced due to the continued evolution of this manufacture process technologies [19]. The key analog building block used in these CMOS ICs is usually the operational transconductance amplifier (OTA), which is implemented with a differential circuit in its input stage [1-9]. The analog electrical performance of the differential circuit crucially depends on how identical or how matched are the devices that compose it, taking into account mainly their dimensions (aspect ratio, W/L, where W and L are respectively the channel width and length) and technological parameters, such as the gate oxide and silicon film thicknesses, and doping concentrations of the drain, channel and source regions, etc. [1-2]. Besides, the devices mismatching is straightforwardly correlated to the differences between their electrical behaviors, which they are implemented with the same geometries, dimensions, and also when they are operating in the same bias conditions, due to the CMOS ICs manufacturing processes variations [1-5].

Lately it was proposed an innovative layout technique to increase the electrical performance of Metal-OxideSemiconductor (MOS) Silicon-On-Insulator (SOI) Field

Effect Transistors (MOSFETs) [10-13], without adding any extra cost to the CMOS ICs manufacturing processes. This happens because the Diamond MOSFETs have two additional effects entitled Longitudinal Corner Effect (LCE), which is responsible to boost the resultant longitudinal electric field along the channel length in relation to the one observed in the CSnM counterpart, regarding the same channel width, gate area $\left(\mathrm{A}_{\mathrm{G}}\right)$, and bias conditions [10-13], and Parallel Association of MOSFETs with Different Channel Lengths Effect (PAMDLE) [10-13]. The hexagonal gate geometry (Diamond layout style) is an example of this layout approach [10-13]. In this circumstances, an experimental comparative study is significant to be done to explore the influence of the Diamond layout style (hexagonal gate shape) [10-13] in the n-type SOI MOSFETs (nMOSFETs) matching in comparison to the traditional rectangular layout style. Fig. 1 shows a photograph of a n-type Diamond SOI MOSFET (DSnM).


Fig. 22 Example of a picture of a DSnM.

In Fig. $1, \mathrm{~b}$ and B are the smallest and highest dimensions of the DSnM channel length, $\alpha$ is the angle between the metallurgical junctions composed by the drain-silicon film (channel)-source regions.

## II. Devices Matching Quantification

The relative error ( $\varepsilon_{\mathrm{r}}$ ) in percentage of the devices matching between the DSnMs and typical rectangular SOI MOSFETs (CSnMs) counterparts, due to the variations of the CMOS ICs manufacturing process, is calculated by Equation (1) [14-15]. The $\varepsilon_{\mathrm{r}}$ states how much the DSnM can present a better $\left(\varepsilon_{\mathrm{r}}<0\right)$ or worse $\left(\varepsilon_{\mathrm{r}}>0\right)$ devices matching in comparison to their CSnM counterparts.

$$
\begin{equation*}
\varepsilon_{r}=\left(\frac{\left(\frac{s_{D S n M}}{x_{D S n M}}\right)-\left(\frac{s_{C S n M}}{x_{C S n}}\right)}{\left(\frac{s_{C S n M}}{x_{C S n}}\right)}\right) \cdot 100 \tag{1}
\end{equation*}
$$

where $\mathrm{s}_{\mathrm{DSnM}}$ and $\mathrm{s}_{\mathrm{CSnM}}$ and $\mathrm{x}_{\mathrm{DSnM}}$ and $\mathrm{x}_{\mathrm{CSnM}}$ are respectively the standard deviations, and the average values of a specific parameter of the DSnMs and CSnMs, considering a devices sample.

## III. Device Description

The DSnM and their CSnM counterparts were manufactured by using $1 \mu \mathrm{~m}$ SOI CMOS manufacturing process from Université catholique de Louvain (ICTEAM/ ELEN, UCL, Belgium). The Keithley 4200 was used to perform the electrical characterization of transistors. The key parameters of the fully depleted SOI nMOSFETs are as follows: the gate oxide thickness ( $\mathrm{t}_{\mathrm{ox}}$ ), silicon film $\left(\mathrm{t}_{\mathrm{SI}}\right)$, and buried oxide ( $\mathrm{t}_{\mathrm{BOX}}$ ) are respectively 30 nm , and 80 $\mathrm{nm}, 390 \mathrm{~nm}$, the doping concentrations of the drain/source and channel are equal to $4 \times 10^{20} \mathrm{~cm}^{-3}$ and $6 \times 1016 \mathrm{~cm}-3$, respectively. The total data sample consists of 9 ICs. We studied 40 transistors per integrated circuit (IC), i.e. 20 pairs of SOI nMOSFETs with the same $\left(\mathrm{A}_{\mathrm{G}}\right): 20 \mathrm{DSnM}$ and 20 CSnM counterparts. From the 40 SOI nMOSFETs studied, there are 4 sets of 5 pairs of SOI nMOSFETs, which present the same $\mathrm{W}(12 \mu \mathrm{~m}, 24 \mu \mathrm{~m}, 30 \mu \mathrm{~m}$, and $180 \mu \mathrm{~m}$, respectively) with different values of the $\alpha$ angles $\left(36.9^{\circ}, 53.1^{\circ}, 90^{\circ}\right.$, $126.9^{\circ}$, and $143.1^{\circ}$, respectively). These accounts a total of 360 transistors analyzed. The average threshold voltage $\left(\mathrm{V}_{\mathrm{TH}}\right)$ of these devices is approximately 0.3 V . The average standard deviation of the $\mathrm{V}_{\text {TH }}$ of the analyzed samples for the DSnM devices, regarding the $\alpha$ angles equal to $36.9^{\circ}$, $53.1^{\circ}, 90^{\circ}, 126.9^{\circ}$ and $143.1^{\circ}$ is equal to 0.17 V , respectively. The average standard deviation of the $\mathrm{V}_{\mathrm{TH}}$ regarding the CSnM devices which are equivalent to the DSnM with $\alpha$ angles equal to $36.9^{\circ}, 53.1^{\circ}, 90^{\circ}, 126.9^{\circ}$ and $143.1^{\circ}$ is equal to 0.15 V , respectively.

For comparison purposes, considering that the DSnMs and their CSnM counterparts present the same W, and AG, the CSnM L must present the average value of the smallest (b) and largest (B) values of the DSnM channel length, according to Equation (2).

$$
\begin{equation*}
\mathrm{L}=\frac{\mathrm{B}+\mathrm{b}}{2} \tag{2}
\end{equation*}
$$

However, the SOI nMOSFET can be represented electrically as the parallel connection of N (integer number) SOI nMOSFETs with trapezoidal (rectangular, if N tends to infinite) gate shapes interconnected in parallel, with a channel width equal to $\mathrm{W} / \mathrm{N}$ and different channel lengths $\left(\mathrm{L}_{1}, \mathrm{~L}_{2}\right.$, $\ldots, \mathrm{L}_{\mathrm{N}}$ ), which vary approximately from baB. Fig. 2 shows how a Diamond SOI nMOSFET can be partitioned into N different SOI nMOSFETs with trapezoidal gate geometries.


Fig. 2 Example of a DSnM partitioned in N SOI nMOSFETs with trapezoidal gate formats.

Fig. 3 illustrates the electrical representation of the Diamond SOI nMOSFET (Fig.3a), where $\mathrm{W} / \mathrm{L}_{\text {eff }}$ is its effective aspect ratio and $L_{\text {eff }}$ is its effective channel length; and its corresponding equivalent electrical circuit, considering that this device is subdivided in N SOI nMOSFETs with trapezoidal (rectangular, if N tends to infinite) gate shapes, which present the same channel widths (W/N) and different channel lengths $\left(\mathrm{L}_{1}, \mathrm{~L}_{2}, \ldots, \mathrm{~L}_{\mathrm{N}}\right)$ (Fig.3b).


Fig. 3 Diamond SOI nMOSFET with its aspect ratio (W/L $\mathrm{L}_{\text {eff }}$ ) (Fig.3.a), and its equivalent electric circuit considering that this device can be partitioned in N SOI nMOSFETs of trapezoidal format, with channel width $\mathrm{W} / \mathrm{N}$ and different lengths $\left(\mathrm{L}_{1}, \mathrm{~L}_{2}, \ldots, \mathrm{~L}_{\mathrm{N}}\right)$ (Fig.3.b).

In Fig. 3, IDS is the drain current of the Diamond SOI nMOSFET, and $\mathrm{I}_{\mathrm{DS} 1}, \mathrm{I}_{\mathrm{DS} 2}$ and $\mathrm{I}_{\mathrm{DSN}}$, are the $\mathrm{I}_{\mathrm{DS}}$ of each SOI nMOSFET with trapezoidal gate geometry.

To obtain a simple first-order model of the $\operatorname{DSnM} \mathrm{L}_{\text {eff }}$ consider Fig. 4, which illustrates a Diamond SOI nMOSFET partitioned into 8 equal parts $(\mathrm{N}=8)$.


Fig. 4 Example of a Diamond SOI nMOSFET segmented into 8 equal parts, representing 8 SOI nMOSFETs with trapezoidal gate geometries, with different channel lengths and with the same channel width (W/N).

In Fig.4, L1, ..., L8 are the average values of channel lengths of the 8 SOI nMOSFETs which are interconnected in
parallel respectively, X 1 is the projection in the x -direction of the base of the triangle 1 , which belongs to the gate region of each one of the SOI nMOSFETs with trapezoidal shape, and $\mathrm{b}, \mathrm{B} 1, \mathrm{~B} 2, \mathrm{~B} 3$ and B are the dimensions of the trapezoidal bases of SOI nMOSFETs that are connected in parallel.

By analyzing the equivalent electrical circuit of Fig. 3, the $\mathrm{DSnM}_{\mathrm{DS}}$ is given by the sum of the $\mathrm{I}_{\mathrm{DS}}$ of each SOI nMOSFET with trapezoidal gate shape (Kirchhoff's Law of Nodes), according to Equation (3), considering N equal to 8 .

$$
\begin{equation*}
\mathrm{I}_{\mathrm{DS}}=\mathrm{I}_{\mathrm{DS} 1}+\mathrm{I}_{\mathrm{DS} 2}+\mathrm{I}_{\mathrm{DS} 3}+\mathrm{I}_{\mathrm{DS} 4}+\mathrm{I}_{\mathrm{DS} 5}+\mathrm{I}_{\mathrm{DS} 6}+\mathrm{I}_{\mathrm{DS} 7}+\mathrm{I}_{\mathrm{DS} 8} \tag{3}
\end{equation*}
$$

Thus, the Diamond SOI nMOSFET $\mathrm{L}_{\text {eff }}$ of the Diamond type considering 8 SOI nMOSFETs interconnected in parallel is given by Equation (4).

$$
\begin{equation*}
L_{e f f}=\frac{8}{2 \cdot\left[\frac{1}{b+\frac{W / 8}{\operatorname{tg}(\alpha / 2)}}+\frac{1}{b+\frac{3 \cdot W / 8}{\operatorname{tg}(\alpha / 2)}}+\frac{1}{b+\frac{5 \cdot W / 8}{\operatorname{tg}(\alpha / 2)}}+\frac{1}{b+\frac{7 \cdot W / 8}{\operatorname{tg}(\alpha / 2)}}\right]} \tag{4}
\end{equation*}
$$

Equation (4) can be generalized according to Equation (5), considering N as an even number and higher than 6 .


To understand numerically what Equation (5) means, Table I illustrates the values of the $\mathrm{DSnM} \mathrm{L}_{\text {eff }}$, considering different values of N .

Table I. Dimensions of DSnMs, their $\mathrm{L}_{\text {eff }}$ [Equation (5)] regarding different N , and the CSnM's Ls, which present the same $\mathrm{A}_{\mathrm{G}}$ of DSnM
counterparts.

| Diamond SOI nMOSFETS dimensions ( $\mu \mathrm{m}$ ) |  |  |  | Effective lenghts of the Diamond SOI nMOSFETs considering the PAMDLE ( $\mu \mathrm{m}$ ) |  | CSnM L that presents the same Ag of a $\mathrm{DSnM}(\mu \mathrm{m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| W | b | N | $\alpha$ ( ${ }^{*}$ | $\mathrm{L}_{\text {eff }}(\mathrm{N}=10)$ | $\mathrm{L}_{\text {eff }}(\mathrm{N}=50)$ | $\mathrm{L}=(\mathrm{b}+\mathrm{B}) / 2$ |
| 12 | 2 | 38 | 36.9* | 13.4 | 12.3 | 20 |
| 12 | 2 | 26 | 53.1* | 9.95 | 9.39 | 14 |
| 12 | 2 | 14 | $90^{*}$ | 6.33 | 6.17 | 8 |
| 12 | 2 | 8 | 126.9* | 4.37 | 4.33 | 5 |
| 12 | 2 | 6 | $143.1{ }^{*}$ | 3.66 | 3.64 | 4 |
| 24 | 4 | 76 | 36.9* | 26.8 | 24.6 | 40 |
| 24 | 4 | 52 | $53.1{ }^{*}$ | 19.9 | 18.8 | 28 |
| 24 | 4 | 28 | $90^{*}$ | 12.7 | 12.3 | 16 |
| 24 | 4 | 16 | 126.9* | 8.74 | 8.66 | 10 |
| 24 | 4 | 12 | 143.1* | 7.32 | 7.29 | 8 |
| 30 | 5 | 95 | 36.9 * | 33.5 | 30.8 | 50 |
| 30 | 5 | 65 | 53.1* | 24.9 | 23.5 | 35 |
| 30 | 5 | 35 | $90^{*}$ | 15.8 | 15.4 | 20 |
| 30 | 5 | 20 | 126.9* | 10.9 | 10.8 | 12.5 |
| 30 | 5 | 15 | $143.1{ }^{*}$ | 9.15 | 9.11 | 10 |
| 180 | 30 | 570 | 36.9 * | 201.2 | 184.5 | 300 |
| 180 | 30 | 390 | 53.1* | 149.2 | 140.9 | 210 |
| 180 | 30 | 210 | $90^{*}$ | 94.9 | 92.6 | 120 |
| 180 | 30 | 120 | 126.9* | 65.5 | 64.9 | 75 |
| 180 | 30 | 90 | 143.1* | 54.9 | 54.6 | 60 |

Observing the results obtained of the values of DSnM $\mathrm{L}_{\text {eff, }}$, we conclude that the hexagonal layout style for SOI nMOSFETs has the capacity to reduce its channel length (L) in relation to a standard SOI nMOSFET (rectangular gate geometry) counterpart, considering that they present the same W, and $\mathrm{A}_{\mathrm{G}}$. This effect is entitled "Parallel connection of MOSFETs with Different Channel Lengths Effect, PAMDLE") [13].

When N in Equation (5) tends to infinite, the $\mathrm{DSnM} \mathrm{L}_{\text {eff }}$ is given by the Equation (6). Besides, the incorporation of the PAMDLE makes the first-order model of the DSnM $L_{\text {eff }}$ more accurate with maximum error of $9.5 \%$ for micrometre scale [13].

$$
\begin{equation*}
L_{e f f}=\frac{B-b}{\ln \left(\frac{B}{b}\right)} \tag{6}
\end{equation*}
$$

## IV. Experimental Results

Table II presents the dimensional characteristics of four pairs of equivalent MOSFETs (rectangular and hexagonal
gate geometries), regarding five different $\alpha$ angles. For instance, considering the first row of Table II, there are four equivalent MOSFETs with rectangular and hexagonal gate geometries with the same $\mathrm{W}(12,24,30$ and $180 \mu \mathrm{~m})$ and $\mathrm{A}_{\mathrm{G}}\left(240,960,1500\right.$, and $54000 \mu \mathrm{~m}^{2}$ ). Besides, we have four different L for the four CSMs (20, 40, 50, and 300 $\mu \mathrm{m})$ and four b $(2,4,5$, and $30 \mu \mathrm{~m})$, B ( $38,76,95$, and 570 $\mu \mathrm{m})$ and $\mathrm{L}_{\text {eff }}(12.3,24.6,30.8$, and $184.5 \mu \mathrm{~m})$ for the four DSM counterparts. As we study five different $\alpha$ angles, the total number of devices investigated were 40 per CMOS IC studied.

Table II. The dimensional characteristics of the devices used for this study.


Regarding Table II, placing the Diamond MOSFET layout over the Rectangular MOSFET one (overlap), it is possible to analyze if their total areas are similar, as illustrated in Fig. 5.


Fig. 5 Overlapping of the layouts of the Diamond and Rectangular MOSFETs in order to verify if their total die areas are similar.

Therefore, according to Fig. 5, it is possible to verify that the area of region 3 is basically the same as the sum of the area of regions 1 and 2 . Therefore, one can conclude that their total die areas are practically the same. Additionally, it is also possible to affirm that the same behavior happens concerning region 6 , that is, the sum of the areas of regions 4 and 5 are practically the same as the area of region 6 .

By analyzing the IDS as a function of the drain voltage $\left(\mathrm{V}_{\mathrm{DS}}\right)$ of 360 SOI nMOSFETs indicated in Table II, in the moderate inversion regime, the devices matching of DSnMs in relation to the CSnM counterparts, concerning the saturation drain current $\left(\mathrm{I}_{\text {Dssat }}\right)$ normalized as a function of the aspect ratio (AR) $\left[\varepsilon_{r_{\_} \operatorname{DSsat}(\text { (AR })}\right]$, taking into account only the LCE effect ( $\mathrm{W} / \mathrm{L}_{\text {eff }}$ ), and also considering the two effects (LCE and PAMDLE) working simultaneously (W/L), where L corresponds to the channel length of a standard (rectangular gate geometry) SOI nMOSFET, which presents the same W,
and $\mathrm{A}_{\mathrm{G}}$ of a DSnM (real condition of operation), is presented in Fig. 6, regarding $\mathrm{V}_{\mathrm{GS}}$ equal to 0.4 V . The method used to obtain the $I_{D S s a t}$ is described in the references [16-18].


Fig. 6 The $\left[\varepsilon_{\left.r_{\text {IDSsat (AR) }}\right]}\right]$ in relation to the $\alpha$ angles of DSnMs, regarding $\mathrm{V}_{\mathrm{DS}}$ and VGS equal to 1 V and 0.4 V , respectively.

Based on Fig. 6, taking into account the $I_{D S s a t} / A R$, we can see that the DSnMs , considering all $\alpha$ angles studied, are able to present better devices matching in relation to those found with the CSnM counterparts $(-6.3 \%$ for the $\alpha$ equals to $36.9^{\circ},-46.2 \%$ for the $\alpha$ equals to $53.1^{\circ},-18.9 \%$ for the $\alpha$ equals to $90^{\circ},-1.5 \%$ for the $\alpha$ equals to $126.9^{\circ}$ and around $-33.4 \%$ for the $\alpha$ equals to $143.1^{\circ}$ ). This happens because the DSnMs always present higher $\mathrm{I}_{\mathrm{DSsat}} / \mathrm{AR}$ values than those found considering the CSnM counterparts, regarding the same W, AG, and bias conditions, as a result of the LCE and PAMDLE effects. Additionally, in this case, the devices matching related to the $\mathrm{I}_{\mathrm{DSsat}} / \mathrm{AR}$, considering the AR with the presence of both effects (LCE and PAMDLE), which is the real condition of DSnM operation, is similar to that concerning only the LCE effect. This can be justified because both the average values and standard deviations depend on the AR values, which they are changing at the same time, and therefore, the relative error $\left(\varepsilon_{r_{-I D S s a t A R}}\right)$ tends to present similar results.

Fig. 7 illustrates the $\varepsilon_{\mathrm{r}}$ of the maximum transconductance normalized by the aspect ratio $\left[\varepsilon_{\mathrm{r} \text { gmsat/(AR) }}\right]$, considering the LCE and PAMDLE effects and only the LCE effect, of the DSnMs in relation to the CSnM counterparts as a function of the $\alpha$ angles of the DSnMs , regarding $\mathrm{V}_{\text {GS }}$ equal to 0.4 V (saturation region). Therefore, these values correspond to the maximum values of the parameter gm when the MOSFETs are operating in the saturation region. The method used to get the $\mathrm{gm}_{\text {SAT }}$ is defined in the references [16-18].


Fig. 7 The $\left[\varepsilon_{\mathrm{r}_{-\mathrm{gmSAT} /(A R)}}\right]$, considering the LCE and PAMDLE effects and only the LCE effect, in relation to the $\alpha$ angles of DSnMs, regarding $V_{D S}$ and $\mathrm{V}_{\mathrm{GS}}$ equal to 1 V and 0.4 V , respectively.

By analyzing Fig. 7, we can see that the DSnMs with $\alpha$ angles equal to $90^{\circ}$ and $126.9^{\circ}$, respectively, are able to present better devices matching than those obtained with the CSnM counterparts ( $-23.7 \%$ for the $\alpha$ equals to $90^{\circ}$ and $-18.6 \%$ for the $\alpha$ equals to $126.1^{\circ}$ ). This can be explained because the LCE and PAMDLE effects, which are responsible to boost the $\mathrm{DSnMs}^{\prime} \mathrm{gm}_{\mathrm{SAT}} / \mathrm{AR}$ in relation to those found in the CSnMs counterparts, and consequently the average value of the $\mathrm{DSnMs}^{\prime} \mathrm{gm}_{\mathrm{SAT}} / \mathrm{AR}$ is higher than the one observed of the CSnM counterparts, considering the Equation (5). Besides, for the $\alpha$ equal to 53.10 and $143.1^{\circ}$, they present similar devices matching in comparison to their CSnM counterparts ( $-1.9 \%$ for the $\alpha$ equals to $53.1^{\circ}$, and $+3.3 \%$ for $\alpha$ equals to 143.10). Regarding the DSnM with $\alpha$ equal to 53.1 o , although they have greater $\mathrm{gm}_{\mathrm{SAT}} / \mathrm{AR}$ values than those found in the CSnM counterparts, a possible explanation for this effect is due to their geometric shapes (hexagonal) be pointed, and therefore these transistors tend to be more affected by CMOS ICs manufacturing processes variations. Considering the DSnMs with $\alpha$ equal to $143.1^{\circ}$, this can be justified because the DSnMs tend to present an electrical behavior similar to those found in the CSnM counterparts, because the LCE and PAMDLE effects are not so intense and therefore their average values must be similar. Finally, the worst devices matching observed (around $+54.9 \%$ ) in relation to the CSnM counterparts, is related to the DSnMs with $\alpha$ angle equal to $36.9^{\circ}$. This can be justified due to their gate geometries are very pointed, and consequently their $\mathrm{gm}_{\mathrm{SAT}} /$ AR are strongly affected by the manufacturing processes variations (round corners, etc.) [3-5], as illustrated in Fig. 8, although they present higher $\mathrm{gm}_{\mathrm{SAT}} / \mathrm{AR}$ than those found in the CSnM counterparts, as a consequence of the LCE and PAMDLE effects.

Furthermore, the behavior of the devices matching related
to the DSnMs $\mathrm{gm}_{\mathrm{SAT}} / \mathrm{AR}$ in comparison to those presented with the CSnM counterparts, taking into account the LCE and PAMDLE effects together, and only considering the LCE effect, are the same presented to the $\mathrm{DSnMs}^{\prime} \mathrm{I}_{\mathrm{DSsat}} / \mathrm{AR}$.

Fig. 8 illustrates the pointed region of the interface between the source and channel regions of the DSnM with an $\alpha$ angle equal to $36.9^{\circ}$.


Fig. 8 Pointed region of the interface between the source and channel regions of the DSnM with an $\alpha$ angle equals to $36.9^{\circ}$, which presents rounded corner and consequently can be strongly affected by the manufacturing process variations.

The $\varepsilon_{\mathrm{r}}$ of the unit voltage gain frequency $\left[\mathrm{f}_{\mathrm{T}}=\mathrm{gm} /\left(2 \pi \mathrm{C}_{\mathrm{L}}\right.\right.$, where $\mathrm{C}_{\mathrm{L}}$ is the load capacitance adopted equal to 10 pF ] of the DSnMs in relation to the one found with the CSnM counterparts $\left[\varepsilon_{\mathrm{r} \text { ft/(AR) }}\right]$ as a function of the $\alpha$ angles, considering VDS and VGS equal to 1 V , and 0.4 V respectively (Saturation region and moderate inversion regime), concerning both AR normalizations (LCE and PAMDLE effects working together, and considering only the LCE effect acting in the DSnMs ) presents the same behavior than the one observed in the $\varepsilon r$ of the maximum transconductance normalized by the aspect ratio $\left[\varepsilon_{\mathrm{rgmSAT} /(A R)}\right]$. This can be justified because $\mathrm{f}_{\mathrm{T}}$ is directly proportional to gm [19].

Fig. 9 illustrates the $\varepsilon_{\mathrm{r}}$ of the ratio between the transconductance and drain current $\left[\varepsilon_{r_{\text {gm/IDS }}}\right.$ ] of the DSnMs in relation to those with the CSnM counterparts, considering LCE and PAMDLE effects working together and also considering only the LCE effect, as a function of the $\alpha$ angles, regarding $\mathrm{V}_{\mathrm{GS}}$ equal to 0.4 V (saturation region). The method applied to acquire the gm/IDS is described in the references [16-19].


Fig. 9 The $\left[\varepsilon_{\mathrm{r} \text { gm/IDs }}\right]$ of the DSnMs in relation to the CSnM counterparts as a function of the $\alpha$ angles, regarding $\mathrm{V}_{\mathrm{GS}}$ equal to 0.4 V and $\mathrm{V}_{\mathrm{DS}}$ equal to 1 V (Saturation region and moderate inversion regime).

Analyzing Fig.9, we observe that the DSnM with the $\alpha$ angle equal to $53.1^{\circ}, 90^{\circ}, 126.9^{\circ}$ and $143.1^{\circ}$, respectively, are capable of presenting a better devices matching ( $-75.8 \%$ for the $\alpha$ equal to $53.1^{\circ},-35.0 \%$ for the $\alpha$ equal to $90^{\circ},-13.7 \%$ for the $\alpha$ equals to $126.9^{\circ}$ and $-39.6 \%$ for the $\alpha$ equals to $143.1^{\circ}$ ) when compared to those obtained to their CSnM counterparts. This can be justified because the DSnMs present the LCE and PAMDLE effects, which are capable of boosting this figure of merit in relation to those observed with the CSnMs counterparts. Finally, to a $\alpha$ angle equal to $36.9^{\circ}$, one can observe a very different behavior in comparison to the other $\alpha$ angles, that is, the DSnM present a worst matching between devices ( $+16.4 \%$ ) in relation to those obtained to their CSnM counterparts. This can be justified due to the strong influence of the manufacturing process in the gate hexagonal geometries of the DSnMs (rounding corners, doping concentration variation, mobility variations of the charge mobile carriers in this region, etc.) [3-5]. In this case both gm and IDS depends on AR, consequently there are no differences between the relative errors taking into account the LCE and PAMDLE effects working together (real condition) and the $\varepsilon r$ that considers only the LCE effect.

Another important analog figure of merit is the Early voltage $\left(\mathrm{V}_{\mathrm{EA}}\right)$, as the intrinsic voltage gain $\left[\mathrm{A}_{\mathrm{V}}=\left(\mathrm{gm} / \mathrm{I}_{\mathrm{DS}}\right) \cdot \mathrm{V}_{\mathrm{EA}}\right]$ of SOI nMOSFETs is directly proportional to the $\mathrm{V}_{\mathrm{EA}}$ [1920]. Fig. 10 presents the $\varepsilon_{\mathrm{r}}$ of the Early voltages $\left[\varepsilon_{\mathrm{r}-\mathrm{VEA} /(\mathrm{AR})}\right]$ of the DSnMs in relation to the CSnM counterparts, taking into account the LCE and PAMDLE effects acting together and only considering the influence of the LCE effect $\left[\varepsilon_{r-\text { VEA }}\right.$ ${ }_{(\mathrm{L})}$ ] as a function of the $\alpha$ angles, regarding $\mathrm{V}_{\mathrm{DS}}$ equal to 1 V and $\mathrm{V}_{\mathrm{GS}}$ of 0.4 V (Saturation region and moderate inversion regime). The method used to obtain the $\mathrm{V}_{\mathrm{EA}}$ is explained in the references [16-19].


Fig. 10 The $\left[\varepsilon_{r-V E A /(A R)}\right]$ and $\left[\varepsilon_{r-V E A /(L)}\right]$ of the $\operatorname{DSnM} V_{E A}$ in relation to that found with the CSnM counterparts as a function of $\alpha$ angles, regarding $\mathrm{V}_{\mathrm{DS}}$ and $\mathrm{V}_{\mathrm{GS}}$ equal to 1 V and 0.4 V , respectively (Saturation region and moderate inversion regime).

By analyzing Fig.10, we can observe that the devices matching regarding the $\mathrm{V}_{\mathrm{EA}} / \mathrm{AR}$ of the DSnMs in relation to the one found with the CSnMs counterparts are regarding $\alpha$ angles equal to 53.1 o (maximum relative error of $+0.5 \%$ ), $90^{\circ}(-4.0 \%), 126.9^{\circ}(-0.4 \%)$, and 143,10 (maximum relative error of $+6.6 \%$ ), respectively, as regarding the LCE and PAMDLE effects. This can be explained because as the relative error of $\mathrm{DSnMs} \mathrm{V}_{\mathrm{EA}} /(\mathrm{AR})$ increases (standard deviation increases and the average value reduces), and in the same time, the relative error of $\mathrm{CSnMs} \mathrm{V}_{\mathrm{EA}} /(\mathrm{AR})$ reduces (standard deviation reduces and the average value increases) as the $\alpha$ angle reduces. However, for the DSnM with $\alpha$ angle equal to 36.9 o ( $+83.7 \%$ ), the standard deviation of the $\mathrm{V}_{\mathrm{EA}} / \mathrm{AR}$ is very higher than the one found with the CSnM counterpart. Furthermore, we can observe that the devices matching regarding the $\mathrm{V}_{\mathrm{EA}} / \mathrm{L}$ of the DSnMs in relation to the one found with the CSnMs counterparts are, regarding $\alpha$ angles equal to 36.9 o (maximum relative error of $-74.4 \%$ ), 53.10 (-86.5\%), $90^{\circ}(-75.9 \%), 126.9^{\circ}(-89.9 \%)$, and $143,1 \mathrm{o}$ ( $-34.5 \%$ ), respectively, as regarding the LCE effects. This can be explained because $\mathrm{V}_{\mathrm{EA}}$ is only dependent of L , and as the relative error of $\mathrm{DSnMs} \mathrm{V}_{\mathrm{EA}} /(\mathrm{L})$ decreases (standard deviation decreases and the average value increases), and in the same time, the relative error of $\mathrm{CSnMs} \mathrm{V}_{\mathrm{EA}} /(\mathrm{AR})$ reduces (standard deviation reduces and the average value increases) as the $\alpha$ angle reduces, due to mainly the LCE effect.

Fig. 11 illustrates the $\left[\varepsilon_{-A V /(A R)}\right]$ of the DSnMs in relation to the CSnM counterparts as a function of the $\mathrm{DSnM} \alpha$ angle, regarding $\mathrm{V}_{\mathrm{DS}}$ equal to 1 V and $\mathrm{V}_{\mathrm{GS}}$ equal to 0.4 V (Saturation region and moderate inversion regime) [17]. This figure shows the $\left.\varepsilon r_{\text {AV/(AR }}\right)$, which takes into account the LCE and PAMDLE effects working together (real condition) and also the $\varepsilon r_{-\mathrm{AV} /(\mathrm{L})}$ which considers only the LCE effect.


Fig. 11. The $\left[\varepsilon_{\mathrm{r}_{\text {AV/(AR })}}\right]$ and $\left[\varepsilon_{\mathrm{r} \text { VEA/(L) }}\right]$ in relation to the DSnM $\alpha$ angle, regarding $\mathrm{V}_{\mathrm{DS}}$ and $\mathrm{V}_{\mathrm{GS}}$ equal to 1 V and 0.4 V , respectively (Saturation region and moderate inversion regime).

Analyzing Fig.11, we observe that the devices matching of DSnMs with $\alpha$ angles equal to 53.10 , and 900 , respectively, taking into account the $\mathrm{A}_{\mathrm{v}} / \mathrm{AR}$, is better $(-22.6 \%$ for $\alpha$ of $53.1^{\circ}$, and $-12.8 \%$ for $\alpha$ of $90^{\circ}$ ) than those observed with the CSnMs counterparts. However, the DSnMs with $\alpha$ angles equal to $126.9^{\circ}$, and $143.1^{\circ}$, respectively, present practically the same devices matching for the $\mathrm{A}_{\mathrm{v}} /(\mathrm{AR})$ than those verified with the CSnM counterparts ( -2.13 for $\alpha$ of $126.9^{\circ}$, and $+0.1 \%$ for $\alpha$ of $143.1^{\circ}$ ). This happens due to the influence of the both devices matching taking into account the gm/ IDS and $\mathrm{V}_{\mathrm{EA}} /(\mathrm{AR})$, respectively, according the previous results indicated in Figs. 9 and 10, respectively. Besides, we observe that the devices matching of DSnMs with $\alpha$ angles equal to $36.9 \mathrm{o}, 53.1 \mathrm{o}, 90 \mathrm{o}, 126.9 \mathrm{o}$ and 143.1 o respectively, taking into account the $\mathrm{A}_{\mathrm{V}} / \mathrm{L}$, is better ( $-74.3 \%$ for $\alpha$ of $36.9^{\circ}$, $-90.4 \%$ for $\alpha$ of $53.1^{\circ},-57.2 \%$ for $\alpha$ of $90.0^{\circ},-88.8 \%$ for $\alpha$ of $126.9^{\circ}$ and $-20.9 \%$ for $\alpha$ of $143.1^{\circ}$ ) than those observed with the CSnMs counterparts. This can be explained due to the influence of the both devices matching taking into account the $\mathrm{gm} / \mathrm{I}_{\mathrm{DS}}$ and $\mathrm{V}_{\mathrm{EA}} /(\mathrm{L})$, respectively, according the previous results indicated in Figs. 9 and 10, respectively.

Fig. 12 illustrates the $\varepsilon_{\mathrm{r}}$ of the on-state drain current ( $\mathrm{I}_{\text {on }}$ ) normalized by the aspect ratio ( $\mathrm{I}_{\text {on }} / \mathrm{AR}$ ) as a function of the $\alpha$ angles of the DSnM , regarding $\mathrm{V}_{\mathrm{GS}}$ and $\mathrm{V}_{\mathrm{DS}}$ equal to 0.4 V and 50 mV , respectively. This figure shows both AR normalizations (LCE and PAMDLE effects working together, and considering only the LCE effect acting in the DSnMs) of the DSnMs in relation to the one found with the CSnM counterparts $\left[\varepsilon_{r_{I} \operatorname{lon} /(A R)}\right]$. The method utilized to get the $I_{\text {on }}$ is described in the references [16-18].


Fig. 12 The $\left[\varepsilon_{\mathrm{r} \text { Ion/(AR) }}\right]$ in relation to the $\mathrm{DSnM} \alpha$ angle, regarding $\mathrm{V}_{\mathrm{GS}}$ and $\widetilde{V}_{D S}$ equal to 0.4 V and 50 mV , respectively.

From Fig.12, we observe that the DSnM with $\alpha$ equals to $53.1^{\circ}, 90^{\circ}$ and $143.1^{\circ}$ are capable of presenting a better devices matching as compared to the one found with the CSnM counterparts ( $-52.0 \%$ for the $\alpha$ equals to $53.1^{\circ},-55.5 \%$ for the $\alpha$ equals to $90^{\circ}$ and $-18.6 \%$ for the $\alpha$ equals to $143.1^{\circ}$ ). For the $\alpha$ equals to $126.9^{\circ}$, it is possible to verify that there is a similar matching between devices behavior in relation to its CSnM counterparts (around $+0.7 \%$ ). Finally, for the $\alpha$ equals to $36.9^{\circ}$ it is possible to affirm that the DSnM have a worst matching between devices when compared to its CSnM counterparts for an $\alpha$ equals to $36.9^{\circ}$ (around $+38.2 \%$ ). This behavior of the devices matching taking into account of ION/ $A R$ is the same of the $I_{D S s a t} / A R$, as reported earlier.

Fig. 13 illustrates the $\varepsilon r$ of the on-state resistance $\left(R_{\text {on }}\right)$ normalized in relation to the inverse of the AR $\left[\varepsilon_{\mathrm{r} \text { Ron/(1/AR) }}\right]$ of the DSnMs in relation to the CSnM counterparts, for both 1/ AR normalizations, as a function of the $\alpha$ angles, regarding VGS equal to 0.4 V . The technique used to achieve the $\mathrm{R}_{\text {on }}$ is described in the references [16-18].


Fig. 13 The $\left[\varepsilon_{\mathrm{r}_{-} \mathrm{RDSon}(1 / \mathrm{AR})}\right]$ in relation to the $\mathrm{DSnM} \alpha$ angles, regarding VGS equal to 0.4 V , respectively.

By analyzing Fig.13, it is possible to observe that the DSnM with all the $\alpha$ angles are capable of producing a better matching between devices when compared to those found with the CSnM counterparts ( $-89 \%$ for the $\alpha$ equals to $36.9^{\circ}$, $-25.9 \%$ for the $\alpha$ equals to $53.1^{\circ},-53 \%$ for the $\alpha$ equals to $90^{\circ},-60.8 \%$ for the $\alpha$ equals to $126.9^{\circ}$ and $-11.36 \%$ for the $\alpha$ equals to $143.1^{\circ}$ ). This occurs due to LCE and PAMDLE effects in the DSnMs. Furthermore, in this case, the devices matching related to the $\mathrm{R}_{\text {on }} /(1 / \mathrm{AR})$, considering the AR with the presence of both effects (LCE and PAMDLE), which is the real condition of DSnM operation, is similar to that concerning only the LCE effect. This happens due to both the average values and standard deviations depend on the AR values, which they are changing at the same time, and therefore, the relative error $\left[\varepsilon_{\mathrm{r}_{-\mathrm{IDSsat}(\mathrm{AR})}}\right]$ tends to have similar values.

## V. General Comparative Table of the Studied Electrical Parameters and Figures of Merit

Table III presents the relative errors of the devices matching, regarding all electrical parameters and the figures of merit of the DSnMs in relation to their CSnMs counterparts studied on this work, taking into account different AR normalizations (LCE and the PAMDLE effects, and only considering the LCE effect).

Table III. General comparative Table of the devices matching of the
DSnMs in relation to those obtained with the CSnM counterparts,
regarding the different AR normalizations (LCE and the PAMDLE effects and only considering the LCE effect).

| $\varepsilon_{\mathrm{T}}(\%)$ - LCE + PAMDLE |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $a()$ | 36.9 | 53.1 | 90.0 | 126.9 | 143.1 |
| $\mathrm{I}_{\mathrm{DSsa}} / \mathrm{AR}$ | -6.5 | -46.0 | -19.3 | -1.4 | -27.0 |
| $\mathrm{gm}_{\text {SAT }} / \mathrm{AR}$ | +55.5 | -1.7 | -24.9 | -18.9 | +13.1 |
| $\mathrm{gm} / \mathrm{ISS}^{\text {S }}$ | +16.4 | .75.8 | -35.0 | -13.7 | -39.6 |
| $\mathrm{V}_{\mathrm{EN}} / \mathrm{AR}$ | +83.7 | +0.5 | -4.0 | -0.36 | +6.6 |
| $A_{4} /$ AR | +82.9 | -22.6 | -12.8 | -2.1 | +0.1 |
| $\mathrm{I}_{00} / \mathrm{AR}$ | +38.2 | -52.0 | -55.5 | +0.7 | -18.6 |
| $\mathrm{R}_{00} /(1 / \mathrm{AR})$ | -89.0 | -25.9 | -53.0 | -60.8 | -11.4 |
| Average Value | 25.89 | -31.93 | -29.21 | -13.79 | -10.97 |
| Standard Deviation | 60.50 | 27.73 | 19.63 | 22.05 | 18.91 |
| $\varepsilon_{\mathrm{T}}(\%)$ - LCE |  |  |  |  |  |
| $a()$ | 36.9 | 53.1 | 90.0 | 126.9 | 143.1 |
| $\mathrm{I}_{\mathrm{DSaz}} / \mathrm{AR}$ | -6.3 | -46.2 | -18.9 | -1.5 | -33.4 |
| $\mathrm{gm}_{\text {STT }} / \mathrm{AR}$ | +54.9 | -1.9 | -23.7 | -18.6 | +3.3 |
| $\mathrm{gm} / \mathrm{I}_{\mathrm{DS}}$ | +17.4 | .76.0 | -38.0 | -12.0 | -46.0 |
| $V_{\text {ES }}$ / | -74.4 | -86.5 | -75.9 | -89.9 | -34.5 |
| $A_{1} / \mathrm{L}$ | .74.3 | -90.4 | -57.2 | -88.8 | -20.9 |
| $\mathrm{I}_{00} / \mathrm{AR}$ | +38.0 | -52.2 | -55.1 | +2.6 | -23.3 |
| $\mathrm{R}_{0 \text { ef }} /(1 / \mathrm{AR})$ | -88.0 | -26.0 | -52.0 | -60.7 | -1.1 |
| Average Value | -41.00 | -54.17 | -45.83 | . 38.41 | -22.27 |
| Standard Deviation | 54.49 | 32.73 | 20.14 | 40.46 | 17.99 |

Based on Table III, we conclude that the DSnM with $\alpha$ equal to $90 \square$ can always produce the best devices matching devices (in average $-45.8 \%$ with a standard deviation of $20.1 \%$ ), as compared to those obtained with the CSnM counterparts, for all main electrical parameters and figures of merit considered in this study. Therefore, Diamond layout style can be considered an alternative layout technique to boost the accuracy of the analog and digital SOI CMOS ICs applications.

## VI. Conclusions

This study performed an experimental comparative study of the devices matching among the DSnMs and the CSnM counterparts, regarding the same $\mathrm{W}, \mathrm{AG}$ and bias conditions. The results demonstrated that the DSnM with $\alpha$ angles equal to 90 o are capable of boosting in more than $45 \%$ in average, with a standard deviation of $20.1 \%$, the devices matching in comparison to those observed with the CSnM counterparts.

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